

# Mark Scheme (Results)

Summer 2017

Pearson Edexcel International A Level in Statistics S2 (WST02/01)



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### General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

#### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# June 2017 WST02 STATISTICS 2 Mark Scheme

Question	Scheme	Marks			
1.(a)	$X \sim \operatorname{Po}(\frac{1}{4})$	B1			
	$P(X=0) = e^{-\frac{1}{4}} = 0.778800$ awrt <u><b>0.779</b></u>	B1			
		(2)			
(b)	$[(P(X \ge 1))^3] = (1 - 0.7788)^3 = 0.010823$ awrt <b>0.0108</b>	M1 A1			
		(2)			
(0)	$Y \sim B(7, 0.7788)$	B1ft			
(c)	$P(Y=5) = 7C5 (0.7788)^5 (1 - 0.7788)^2 = 0.294386$ awrt <b>0.294</b>	M1 A1			
		(3)			
(d)	H <sub>0</sub> : $\mu = 8$ or $\lambda = 0.25$ H <sub>1</sub> : $\mu < 8$ or $\lambda < 0.25$	B1			
		(1)			
(a)	$W \sim \text{Po}(8)$	B1			
(e)	$W \sim \text{PO}(8)$ $P(W \le 3) = 0.0424 \ (< 0.05)$	M1			
	$P(W \le 4) = 0.0996 \ (> 0.05)$				
	Largest possible value of $f$ is 3	A1 (2)			
		(3) <b>Total 11</b>			
	Notes				
(a)	1 <sup>st</sup> B1 for writing or using Po( $\frac{1}{4}$ ). May be implied by a correct answer or by awrt	0.78			
(b)	M1 for $(1-0.779)^3$ or $(1 - \text{'their (a)'})^3$				
(c)	B1ft for writing or using B(7, 'their a'). May be implied by M1 scored.				
	M1 for a correct binomial expression for P( $Y = 5$ ) (ft their value of $p$ ). Allow $\binom{7}{2}$ etc or 21				
	May be implied by the correct answer but if $p \neq 0.779$ or better we must see expression				
ALT	They may use $W \sim B(7, \text{``} 1 - \text{their (a)''})$ for B1ft then $P(W = 2)$ for the M1				
(d)	B1 for both hypotheses correct. Must use $\lambda$ or $\mu$ for either 8 or 0.25 [Use of $\leq$ is B0]				
	If (d) is blank but correct hypotheses are seen in (e) can award retrospectively BUT if				
	hypotheses are given in (d) and (e) award this mark for answer in (d).				
(e)	B1 for writing Po(8) can be awarded if seen in (d) (may be implied e.g. by scorin	g M1)			
	M1 for using Po(8) to find a lower-tail critical region				
	Need to see one of the given probability statements <u>or</u> implied by Po(8) <u>and</u> $f = 3$ seen. A1 for $[f] = 3$ but allow $f \le 3$ Correct answer only scores 3/3				
	At for $[j] = 3$ but allow $j \leq 3$ . Correct allower only scores $3/3$ .				

Question	Scheme	Marks	
2. (a)(i)		B1	
(ii)	Prizes are randomly placed in packets.	B1	
	Each packet has a 25% chance of containing a prize	(2)	
	Each <u>packet</u> contains a <u>prize</u> <u>independent</u> ly of others	(2)	
(b)	$P(X=1) = {6 \choose 1} (0.25)(1 - 0.25)^5 [= 0.355957] \text{ or } 0.5339 - 0.1780 [= 0.3559]$	M1	
	P(only 1 box contains exactly 1 prize) = $2P(X=1) (1 - P(X=1)) =$ answer in the range <u><b>0.458~0.459</b></u> (inc)	M1 A1 (3)	
(c)	$P(X \ge 2) = 1 - P(X \le 1) = 1 - 0.5339 = 0.4661$ awrt <u><b>0.466</b></u>	M1 A1 (2)	
(d)	$Y \sim B(80, '0.4661') \rightarrow N(\text{awrt } 37.3, \text{ awrt } 19.9)$ [Calc: 37.285, 19.9078]	B1ft	
	$P(Y \le 30) \approx P\left(Z < \frac{30.5 - '37.3'}{\sqrt{19.9'}}\right)$	M1 dM1A1ft	
	P(Z < -1.52) = 1 - 0.9357 = 0.0643 (calc: 0.064165) awrt <u><b>0.064</b></u>	A1 (5)	
		Total 12	
	Notes		
(a)(i) (ii)	B1 for a completely specified distribution. Condone B(6,25%) must be in (a)(i) B1 for a contextualised reason involving randomness, independence or constant p. Must mention "prize" and "packet" and for constant prob "0.25" in correct sta	•	
(b)	1st M1 for a correct expression for $P(X = 1)$ may use $P(X \le 1) - P(X = 0)$ from to $X \sim B(6, 0.25)$ (May be implied by sight of awrt 0.356 or answer in range) 2nd M1 for writing or using $2P(X = 1)$ (1 – $P(X = 1)$ ) NB M0M1A0 is possible Allow just $2P(X = 1)$ (1 – $P(X = 1)$ ) or a numerical expression with any $p = 0.25$ provided $0$	)	
(c)	M1 for writing or using $1 - P(X \le 1)$ A1 for awrt 0.466 (calc: 0.46606445)		
(d)	1 <sup>st</sup> B1ft for mean = $np$ and variance = $np(1-p)$ where $p$ = 'their (c)' ft their 0.466 Any ft values must be correct to at least 3sf 1 <sup>st</sup> M1 $\pm \left(\frac{29.5 \text{ or } 30 \text{ or } 30.5 - \text{their mean}}{\text{their sd}}\right)$	<i>i</i> ≠ 0.25	
	their sd		
	$2^{\text{nd}}$ M1 dependent on $1^{\text{st}}$ M1 for using a continuity correction $30 \pm 0.5$ $1^{\text{st}}$ A1ft for ( $\pm$ ) correct standardized expression (ft their $\mu$ and $\sigma$ ) or $z = \text{awrt} \pm 1.52$		
	2 <sup>nd</sup> A1 awrt 0.064		
	[Use of $p = 0.25$ giving N(20, 15) can score B0M1M1A1A0 i.e. max 3/5]		
NB	Use of binomial (leads to 0.063398 or 0.063477) but scores 0 marks.		

Question		Sch	ieme		Marks
3. (a)	Using area of triangle:	Solve:		Using integration: $P(X > 4)$	
	$P(X > 4) = \frac{(6-4) \times f(4)}{2}$	$\frac{(6-4)(\frac{3}{2}-1)}{2}$	$\left(-\frac{1}{4}x\right) = \frac{1}{2}x$	$= \int_{4}^{6} \left(\frac{3}{2} - \frac{1}{4}x\right) dx = \left[\frac{3}{2}x - \frac{1}{8}x^{2}\right]_{4}^{6}$	M1
	$=\frac{1}{2}$ [so median of X is 4]	so median	of $X$ is 4]	$=\frac{1}{2}$ [ so median of $X$ is 4]	A1cso (2)
(b)		. 4 0 =			
	$\frac{(4-1)\times(4a+b)}{2} = 0.5 \to 12$	2a + 3b = 1	$\left(\frac{1}{\frac{16a}{2}} + 4b\right)$	$dx = 0.5$ $-(\frac{a}{2} + b) = 0.5 \to 15a + 6b = 1$	M1
	$f(1) = 0 \rightarrow a + b = 0$		f(1) = 0	$\Rightarrow a + b = 0$	M1
	Solving simultaneously: $12a - 3a = 1$		Solving si 15 <i>a</i> – 6 <i>a</i> =	multaneously: = 1	dM1
	$a = \frac{1}{9}  b = -\frac{1}{9}$		$a = \frac{1}{9}$	$b = -\frac{1}{9}$	A1 A1 (5)
(c)	$\int_{1}^{x} \left(\frac{1}{9}t - \frac{1}{9}\right) dt$	or $\int \left(\frac{1}{9}x - \frac{1}{9}\right)$	dx with +	c and $F(1) = 0$ or $F(4) = 0.5$	M1
	$0.5 + \int_{4}^{x} \left(\frac{3}{2} - \frac{1}{4}t\right) dt$	or $\int \left(\frac{3}{2} - \frac{1}{4}x\right)$	dx with +	c and $F(6) = 1$ or $F(4) = 0.5$	M1
	[0]	x	<1		D1
	$\int_{\Gamma(x)} \frac{1}{18} x^2 - \frac{1}{9} x + \frac{1}{18} $ $1 \le x < 4$			B1	
	$F(x) = \begin{cases} 0 & x < 1 \\ \frac{1}{18}x^2 - \frac{1}{9}x + \frac{1}{18} & 1 \le x < 4 \\ \frac{3}{2}x - \frac{1}{8}x^2 - \frac{7}{2} & 4 \le x \le 6 \\ 1 & x > 6 \end{cases}$			A1 (7)	
	1   x > 6			A1 (5)	
	Notes			Total 12	
(a)	Notes  M1 for a correct expr' area above 4 using triangle or correct integral & attempt to integrate A1cso for $\frac{1}{2}$ or $x = 4$ with no errors. NB f(4)=1.5 - 1 = 0.5 or 1.5 - 0.25 $x = 0.5$ is M0A0 Allow use of correct $F(x) = 0.5$ provided $F(4) = 0.5$ not used to establish $F(x)$				
(b)	( )	•	. ,	· · · · · · · · · · · · · · · · · · ·	
	$2^{\text{nd}}$ M1 for a correct equation in $a$ and $b$ using $f(1) = 0$ $3^{\text{rd}}$ dM1 dep on at least 1 M1; for solving two linear equations in $a$ and $b$ by eliminating one variable (allow one slip). If one equation is incorrect we must see explicit method to solve.			nating one l to solve.	
(c)	1 <sup>st</sup> A1 for a and 2 <sup>nd</sup> A1 for b (allow exact equivalents) 1 <sup>st</sup> M1 for attempt to integrate $ax + b$ with correct limits $\underline{\mathbf{or}} + c$ and $F(1) = 0$ $\underline{\mathbf{or}}$ $F(4) = 0.5$ 2 <sup>nd</sup> M1 for attempt to integrate $\frac{3}{2} - \frac{1}{4}x$ with correct limits & $+0.5$ $\underline{\mathbf{or}} + c$ and $F(6) = 1$ $\underline{\mathbf{or}}$ $F(4) = 0.5$				
	For the 2 <sup>nd</sup> M1 allow $\int_{0}^{4} (\text{their } ax + b) dx$ or F(4) based on their cdf for [1, 4) instead of $+0.5$				
	B1 for $1^{st}$ and $4^{th}$ line correct Allow $\leq$ or $\leq$				
	1 <sup>st</sup> A1 correct 2 <sup>nd</sup> line with limits NB $\frac{1}{18}(x-1)^2$ anywhere for				
	2 <sup>nd</sup> A1 correct 3 <sup>rd</sup> line with	limits NB	$1-\frac{1}{8}(x-6)^2$	the last 3 marks	

Question	Scheme	Marks
4. (a)(i)	mean = np = 3.5	B1
(ii)	standard deviation = $\sqrt{700 \times \frac{1}{200} (1 - \frac{1}{200})} = 1.86614$ awrt <u>1.866</u>	M1 A1
		(3)
(b)(i)	$H_0: p = \frac{1}{200}$ $H_1: p > \frac{1}{200}$	B1
(ii)	$X \sim B(500, \frac{1}{200}) \rightarrow Po(2.5)$	B1
	$P(X \ge 5) = 1 - P(X \le 4) = 1 - 0.8912 = 0.1088$	M1 A1
	[0.1088 > 0.05] therefore do not reject H <sub>0</sub> , not significant, 5 does not lie in CR	M1
	The doctor's claim is not supported. <b>or</b> Past records are not out of date/reliable	A1 cso
	or Number/ Proportion / Probability of people/ with allergy is not higher.	(6)
		(0)
(c)	$Y \sim B(n, 0.30)$	
	$P(Y=0) = (0.70)^n < 0.005$	M1
	n > 14.85	
	n=15	A1cao
	$P(Y \geqslant w) < 0.005$	M1
	$P(Y \le 8) = 0.9848 \text{ or } P(Y \ge 9) = 0.0152 [>0.005]$	1 <b>V1</b> 1
	$P(Y \le 9) = 0.9963 \text{ or } P(Y \ge 10) = 0.0037[<0.005]$	A1
	w = 10	
		(4) <b>Total 13</b>
	Notes	10tal 13
(a)(ii)	M1 for a correct expression for standard deviation including root	
	NB Assuming Poisson will get $\sqrt{3.5} = 1.87082$ but scores M0A0 [ Ans only	2/2]
(b)(i)		(i) is B0]
(ii)	B1 for writing or using Po(2.5)	
	1st M1 for $1 - P(X \le 4)$ and use with bin or Poisson or for CR $P(X \ge 6) = 0.042$	<0.05]
	1st A1 for awrt 0.109 or for CR $X \ge 6$	
	2 <sup>nd</sup> M1 for a non-contradictory statement which follows from their probability/CR 2 <sup>nd</sup> A1cso correct contextual statement and fully correct solution with all other	-
	marks scored in (b) (ii)	
NB		
	Use of Normal [ may get 0.103 ( Po) or 0.102 (bin)] in (b) can score B1B0M0A0	M1A0
(c)	1 <sup>st</sup> M1 for a correct expression for $P(Y = 0)$ and comparison with 0.005	
	[allow inequality or equation]. Use of tables alone is M0	. 0 0051
	$1^{\text{st}}$ A1 for $n = 15$ cao [ Answer only is M0A0 unless we see the $0.7^n$ compared to $2^{\text{nd}}$ M1 for using B("15", 0.30) to try and find an upper tail, need sight of <u>one</u> of g	
ft	If $1^{st}$ M1 scored can ft their <i>n</i> but need sight of probability expression and probability expre	
10	one of which must be a correct ft and must be just above or just below 0.005 (o.e.	•
	$2^{\text{nd}} \text{ A1 for } w = 10 \text{ [but } w \geqslant 10 \text{ is A0]} \text{ Allow } Y \geqslant 10 \text{ or } Y > 9$	,
	[ Correct answer only scores M0A0M1A1]	

Question	Scheme	Marks	
5. (a)	P(customer waits > 4 minutes) = $1 - F(4) = 1 - [0.3(4) - 0.004(4^3)] =$	M1	
	$\frac{7}{125}$ or $0.056$	A1	
		(2)	
(b)	P(customer waits > 4 minutes   customer waits > 2 minutes) =		
	$\frac{P(T>4)}{P(T>2)} = \frac{"0.056"}{1-F(2)}, = \frac{"0.056"}{1-[0.3(2)-0.004(2^3)]} = \frac{"0.056"}{0.432} =$	N/1 A 1.C	
	$P(T > 2)$ $1 - F(2)^{2}$ $1 - [0.3(2) - 0.004(2^{3})]$ 0.432	M1,A1ft	
	$\frac{7}{54}$ or awrt <b>0.130</b>	A1	
	54	(3)	
(c)	F(2.7) = 0.73(1268) or $F(2.7) - 0.75 = -0.02$	M1	
	F(2.8) = 0.752(192) or $F(2.8) - 0.75 = (+) 0.002$		
	F(2.7) < 0.75 < F(2.8) therefore 2.7 < upper quartile < 2.8	A1cso	
	(2.1) (2.10) moretere 2.1, apper quantité 2.10	(2)	
(d)	$f(t) = 0.3 - 0.012 t^2$	M1	
	$E(T) = \int_{0}^{5} t(0.3 - 0.012t^{2}) dt = \left[\frac{0.3t^{2}}{2} - \frac{0.012t^{4}}{4}\right]_{0}^{5} , = \frac{0.3 \times 5^{2}}{2} - \frac{0.012 \times 5^{4}}{4}$	N/1 A 1	
	$E(T) = \int_{0}^{1} t(0.3 - 0.012t^{2}) dt = \frac{1}{2} - \frac{1}{4} = \frac{1}{2} - \frac{1}{4}$	M1, A1	
	$=\frac{15}{8}$ or 1.875	A1	
	o a constant of the constant o	(4)	
		Total 11	
	Notes		
(a)	M1 for writing or using $1 - F(4)$ [Just writing $F(4) = 0.944$ alone is M0]		
(b)	M1 for a correct ratio expression $\frac{P(T > 4)}{P(T > 2)}$ or $\frac{"(a)"}{P(T > 2)}$ or better. Ignore e.g. $P(T > 2)$	T > 2 T > 4	
	Allow other letters for $T$ . If <u>only</u> numerical values are used, must have num <		
	1 <sup>st</sup> A1ft for a correct ratio expression with 'their (a)' on numerator and correct numerical		
	expression or 0.43 or better on denominator.		
	M1 for attainmting to find E(2.7) and E(2.9)		
(c)	M1 for attempting to find $F(2.7)$ and $F(2.8)$ A1cso for both $F(2.7) = \text{awrt } 0.73 < 0.75 < F(2.8) = \text{awrt } 0.752$ and correct conclusions.	sion	
	May use $F(x) = 0.75$ and look for a change of sign. There must be sight of (		
ALT	Using calculator: M1 for $0.3t - 0.004t^3 = 0.75$ leading to $t = \text{awrt } 2.79$ (2.78937		
	A1 for correct conclusion (must reject other roots i.e. $6.9218$ and $-9.7112$ if for	•	
	Conclusion must clearly state that $Q_3$ is between 2.7 and 2.8. Penalise false st	atements.	
(d)	$1^{st}$ M1 for differentiating F(t) to find f(t) [ Just 2 terms with at least 1 correct]		
(u)	2 <sup>nd</sup> M1 for attempting to integrate $t \times$ their $f(t)$ ignore limits[ at least one $t^n \to t^{n+1}$ ]		
	1 <sup>st</sup> A1 for correct integration of correct $f(t)$ & use of limits (must see some correct		
	This mark may be implied by a correct answer.	/	
	$2^{\text{nd}} \text{ A}1 \frac{15}{8} \text{ or } 1.875 \text{ (condone } 1.88) \text{ [Correct answer only of } \frac{15}{8} \text{ or } 1.875 \text{ scores } 4$	1/41	
	$\frac{2}{8}$ $\frac{61}{8}$ 1.873 (collidered 1.88) [Collect allswell only of $\frac{61}{8}$ $\frac{61}{8}$ 1.873 scores 2	+/ → ]	
Special	Use of $E(T) = 5 - \int_{0}^{5} F(t) dt$ can score 4 out of 4 if fully correct.		
Case	Use of $E(I) = 3 - \int_{0}^{1} F(I)dI$ can score 4 out of 4 if fully correct.		
	U		

Question	Scheme			
6. (a)	(3, 3, 3) $(3, 3, 4) \times 3$ [ $(3, 4, 3), (4, 3, 3)$ ] $(3, 4, 4) \times 3$ [ $(4, 3, 4), (4, 4, 3)$ ] (4, 4, 4)	B1B	1	
(b)	$P(M=3) = (0.5)^3 = 0.125$	B1	(2)	
	$P(M=5) = 1 - (0.8)^{3} \text{ or } P(M=5) = 3(0.2)(0.8)^{2} + 3(0.2)^{2}(0.8) + (0.2)^{3}$ or $P(M=4) = 3(0.5)^{2}(0.3) + 3(0.5)(0.3)^{2} + (0.3)^{3}$	M1		
	P(M=4) = 1 - [(P(M=3) + P(M=5))]  or  P(M=5) = 1 - [(P(M=3) + P(M=4))]	M1		
	$ \begin{array}{ c c c c c c } \hline m & 3 & 4 & 5 \\ \hline P(M=m) & 0.125 & 0.387 & 0.488 \\ & \left(\frac{1}{8}\right) & \left(\frac{387}{1000}\right) & \left(\frac{61}{125}\right) \\ \hline \end{array} $	A1		
(c)	Mode of $\underline{S_1 = 3}$ and Mode of $\underline{M = 5}$	B1	<ul><li>(4)</li><li>(1)</li></ul>	
		Tota	ıl 7	
	Notes (2.2.2)			
(a)	$1^{\text{st}}$ B1 for at least 4 correct samples listed e.g. $(3, 3, 3)$ and $(3, 3, 4) \times 3$ $2^{\text{nd}}$ B1 for all 8 correct samples listed (with no extra or incorrect ones given)			
(b)	B1 for $P(M=3) = 0.125$ oe Condone e.g. $X = 3$ and $12.5\%$ $1^{st}$ M1 for a correct expression or a correct probability for $P(M=5)$ or $P(M=4)$ $2^{nd}$ M1 for a correct expression for third probability of 3, 4 or 5 or if B1 or $1^{st}$ M1 are scored then award this mark for using the sum of the probs = 1 A1 for both $P(M=4) = 0.387$ oe and $P(M=5) = 0.488$ oe			
(c)	B1 for both correct modes with clear $S$ and $M$ labels			

Question	Scheme	Marks	
7.(a)	$E(3-2X)=3-2E(X) = 3-2(\frac{(a+b)}{2})$	M1	
	= 3 - a - b	A1	
	<del></del>	(2)	
(b)	$P(X > \frac{1}{3}b + \frac{2}{3}a) =$		
	$\frac{b-(\frac{1}{3}b+\frac{2}{3}a)}{a}$ , $=\frac{2}{a}$ or $1-\frac{(\frac{1}{3}b+\frac{2}{3}a)-a}{a}$ , $=\frac{2}{a}$	N/1 A 1	
	$\frac{b - (\frac{1}{3}b + \frac{2}{3}a)}{b - a}, = \frac{2}{3} \qquad \text{or} \qquad 1 - \frac{(\frac{1}{3}b + \frac{2}{3}a) - a}{b - a}, = \frac{2}{3}$	M1, A1	
		(2)	
(c)	$[Var(X) = E(X^{2}) - [E(X)]^{2}]$		
	$E([3]X^{2}) = \int_{a}^{b} \frac{1}{(b-a)}[3]x^{2} dx$ $\frac{(b-a)^{2}}{12} = E(X^{2}) - 0^{2} \text{ or } E(X^{2}) - \frac{(a+b)^{2}}{4}$	M1	
	$\frac{1}{a} = E(X^2) - 0^2 \text{ or } E(X^2) - \frac{1}{4}$	1411	
	$= \left[\frac{1}{(b-(-b))} x^{3}\right]_{b}^{b} = \left(\frac{b^{3}-(-b^{3})}{2b}\right)$ $= b^{2}$ $= b^{2}$ $E(3X^{2}) = 3\left(\frac{(b-(-b))^{2}}{12}\right)$ $= b^{2}$	dM1	
	$=b^2$ $=b^2$	A 1	
	<u>l</u>	A1 (3)	
(d)	Range = $b - a = 18$ or $b - b = 18$ or $b = 9$	M1	
, ,	$\begin{bmatrix} 18^2 & 9^2 & 2 \end{bmatrix}$		
	$Var(X) = \begin{bmatrix} \frac{18^2}{12} & \underline{or} & \frac{9^2}{3} - 0^2 \end{bmatrix} = \underline{27}$	A1	
		(2)	
		(2) <b>Total 9</b>	
	Notes	10001	
(a)	M1 for using $3 - 2E(X)$ where $E(X)$ is a linear function of $a$ and $b$		
	A1 for $3 - a - b$ or $3 - (a + b)$		
(b)	M1 C	1 1 (1)	
(b)	M1 for a correct fraction expression for $P(X > \frac{1}{3}b + \frac{2}{3}a)$ in terms of a and b (need	brackets!)	
	A1 for $\frac{2}{3}$		
	3		
(c)	$1^{\text{st}}$ M1 for a correct integral for E(3 $X^2$ ) or E( $X^2$ ) (ignore limits)		
	$2^{\text{nd}}$ dM1 dependent on $1^{\text{st}}$ M1 for correct integration and correct use of $a = -b$ incl	uding in	
	limits. Must be $E(3X^2)$	luding in	
ALT	$1^{\text{st}}$ M1 for a correct expression for E(3X <sup>2</sup> ) or E(X <sup>2</sup> ) in terms of a and b from substant	stituting	
	into $Var(X)$ and using $E(X) = 0$ or $\frac{(a+b)}{2}$		
	<del>-</del>		
	$2^{\text{nd}}$ dM1 dependent on $1^{\text{st}}$ M1 for $3 \text{ E}(X^2)$ and correct use of $a = -b$		
(4)	M1 for writing or using $(b, a) = 18$ or $b = 19$ or $b = 0$		
(a)			
(d)	M1 for writing or using $(b-a) = 18$ or $b-b=18$ or $b=9$ A1 for 27 [Correct answer only is $2/2$ ]		

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